



# SIGGRAPHASIA2009

革新の波動  
*the pulse of innovation*



# Amortized Supersampling

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# Outline

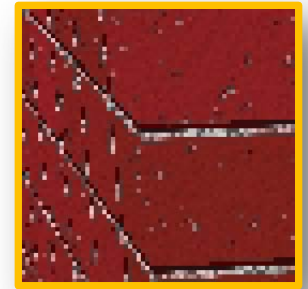
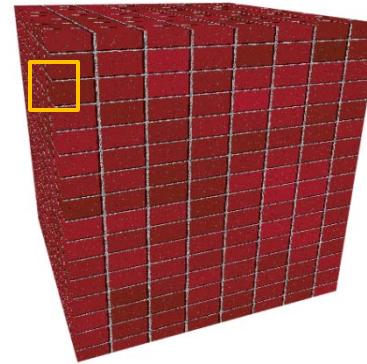
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- Problem
- Amortized supersampling – basic approach
- Challenge - the resampling blur
- Our algorithm
- Results and conclusion

# Problem

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- Shading signals not band-limited
  - Procedural materials
  - Complex shading functions
- Band-limited version (analytically antialiased)
  - Ad-hoc
  - Difficult to obtain



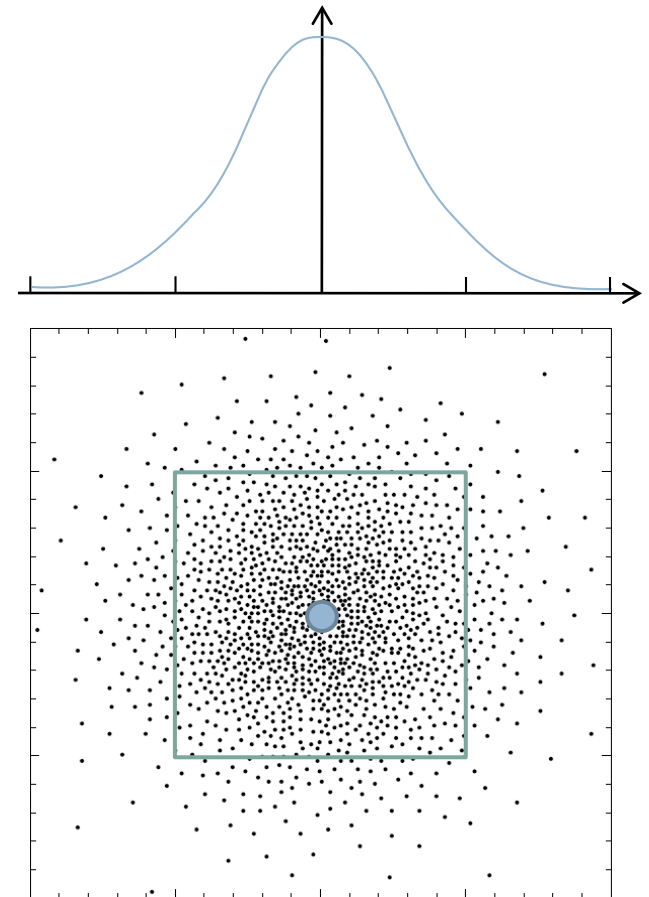
# Problem

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- ▣ Supersampling
  - ▣ General antialiasing solution
  - ▣ Compute a Monte-Carlo estimator

$$f_N[p] \leftarrow \frac{1}{N} \sum_{i=1}^N s_t[p]$$

- ▣ Can be prohibitively expensive

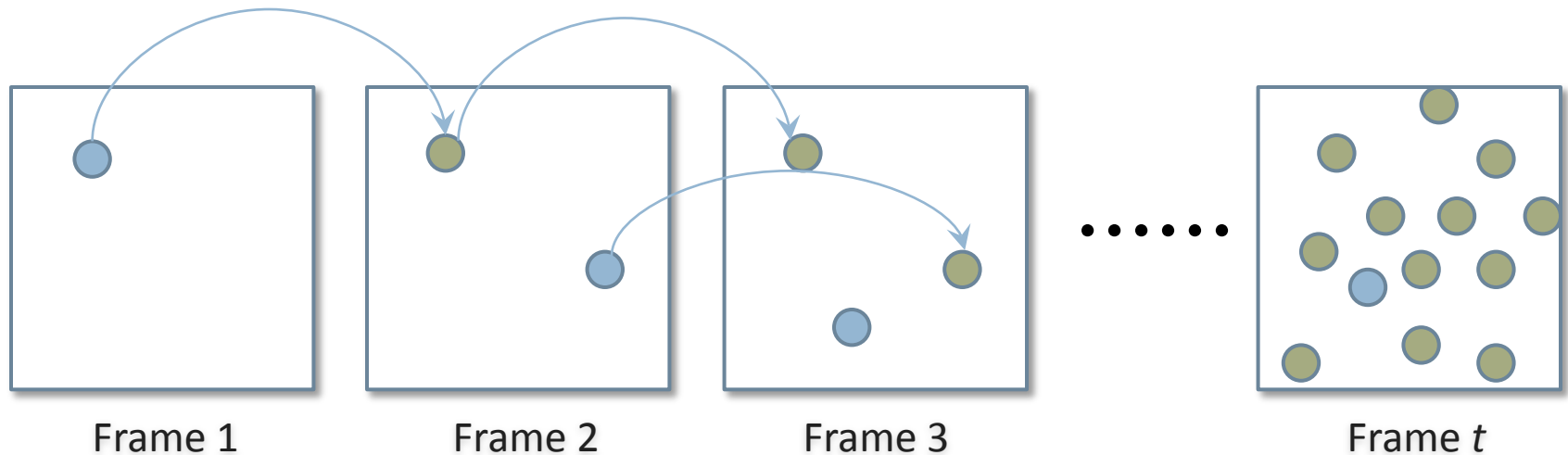




# Accelerating Supersampling

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- ▣ Shading functions usually vary slowly over time
- ▣ Reuse samples from previous frames
  - ▣ Reprojection
  - ▣ Generate only one sample every frame

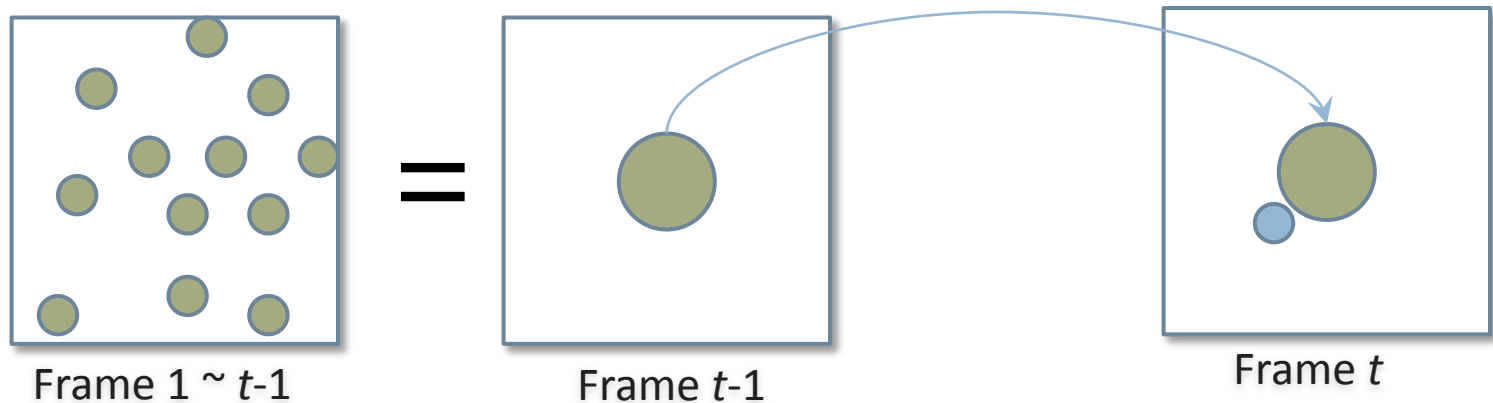


# Amortized Supersampling

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- ❑ Cannot afford to store all the samples from history
- ❑ Keep only a running tally  $f_t$  per pixel
  - ▣ Update it every frame using exponential smoothing

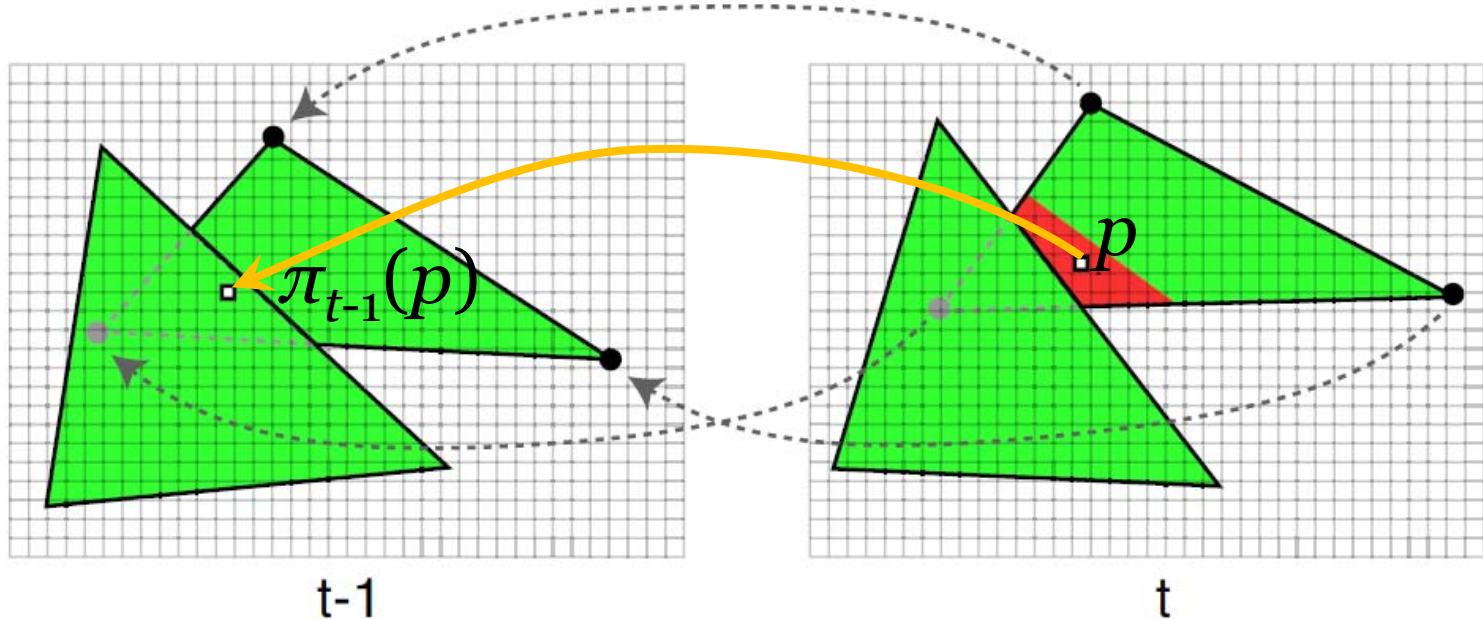
$$f_t[p] \leftarrow (\alpha) s_t[p] + (1 - \alpha) f_{t-1}(\pi_{t-1}(p))$$



# Reverse Reprojection [Nehab07, Scherzer07]

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- Compute previous location  $\pi_{t-1}(p)$  of point  $p$
- A bilinear texture fetch for the previous value  $f_{t-1}(\pi_{t-1}(p))$ 
  - ▣ Check depth for occlusion changes

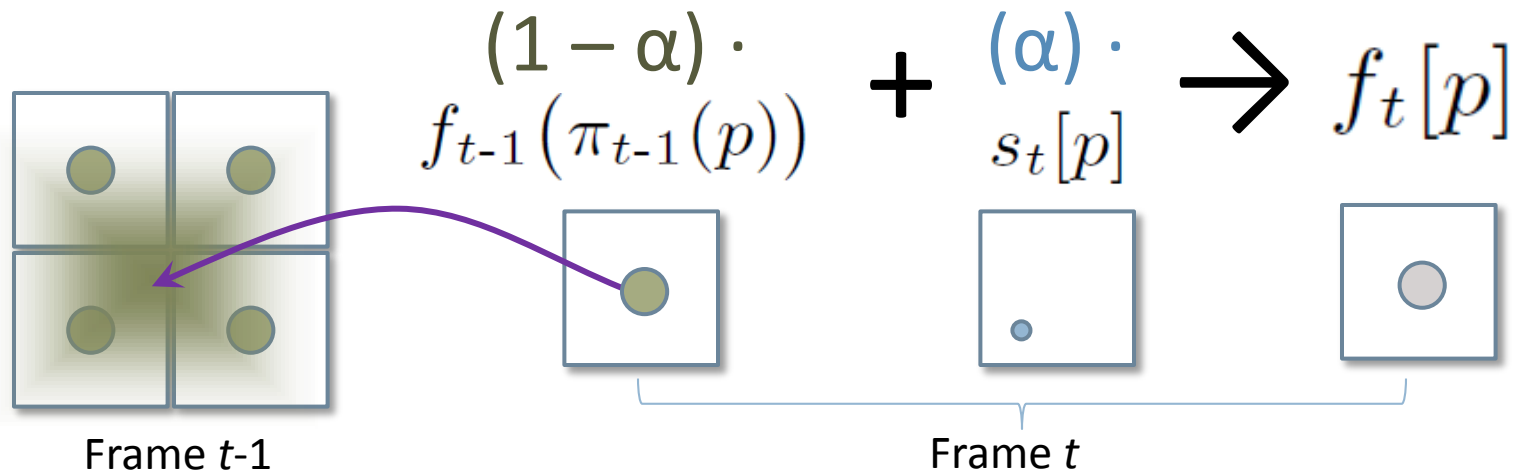




# Effect of the smoothing factor $\alpha$

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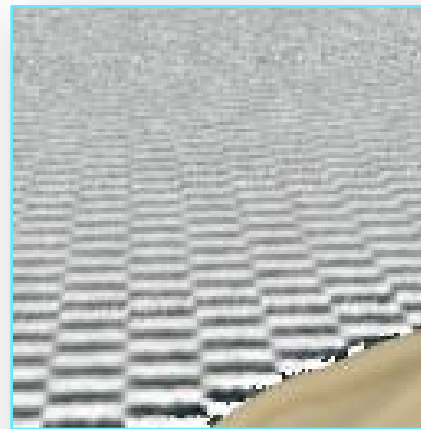
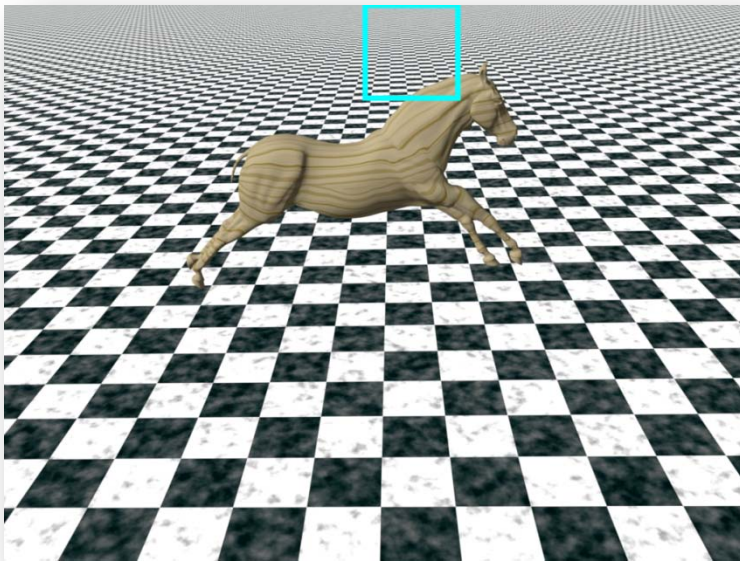
- Larger  $\alpha$ : less history, more aliasing/noise
- Smaller  $\alpha$ : more history, less aliasing/noise
- Equal weight of samples:  $\alpha = \frac{1}{t}$



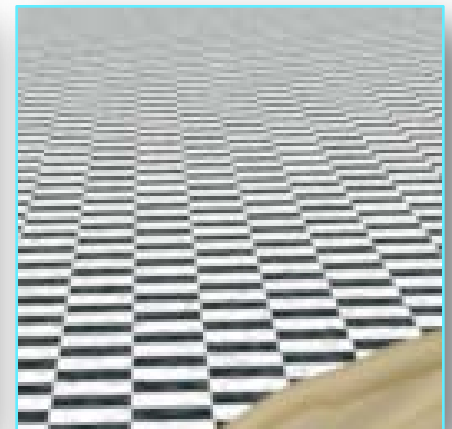
# An artifact of recursive reprojection

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- Blur due to repeated bilinear interpolation



SS through  
Reprojection

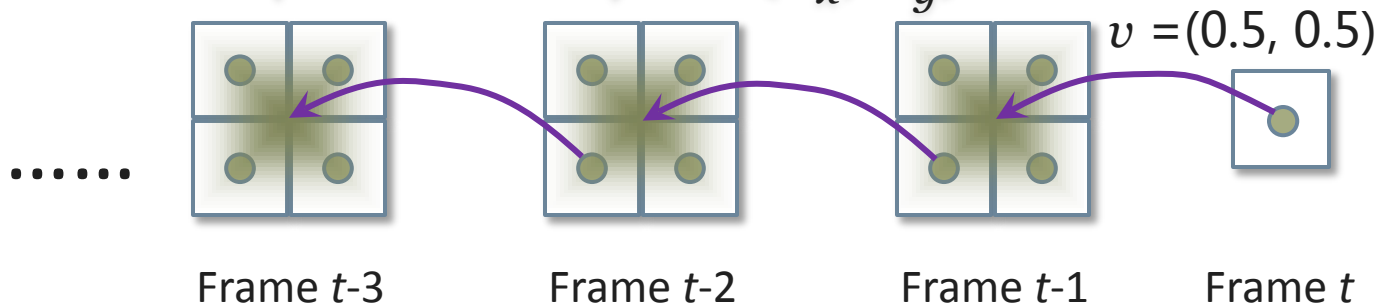


Ground truth

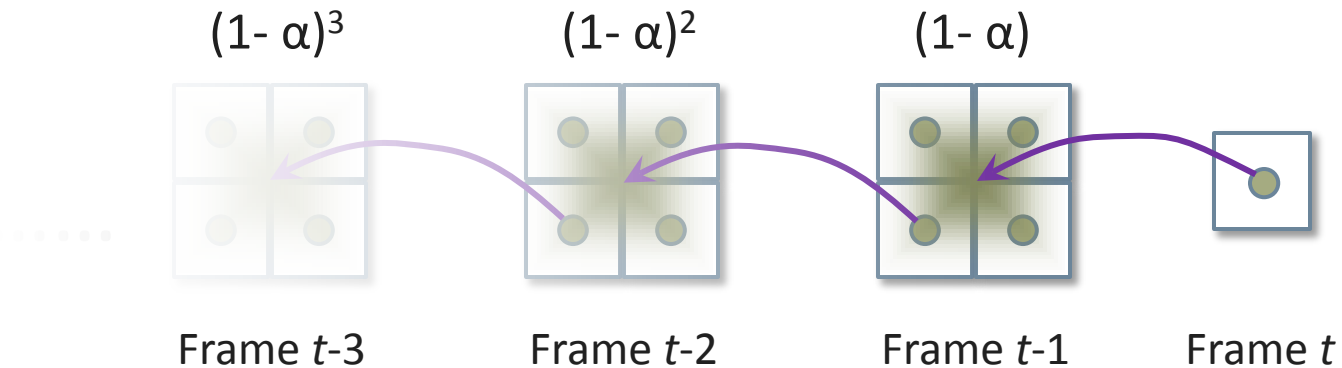
# Factors of the blur

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- Fractional pixel velocity  $v = (v_x, v_y)$



- Exponential smoothing factor  $\alpha$



# The amount of blur

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- The expected blur variance is (derivation in the appendix)

$$\sigma_v^2 = \sigma_G^2 + \frac{1 - \alpha}{\alpha} \frac{v_x(1 - v_x) + v_y(1 - v_y)}{2}$$

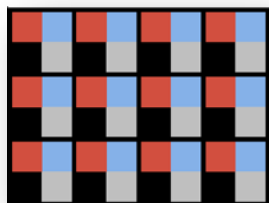
- Approaches for reducing the blur:
  1. Increase resolution of the history buffer
  2. Avoid bilinear resampling whenever possible
  3. Limit  $\alpha$  when needed

# (1) Increase resolution

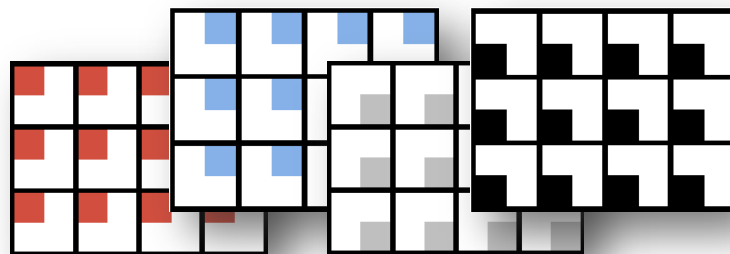
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- Option 1:  
Keep a history buffer at high resolution (2x2)
  - ▣ Have to update it every frame ☹️
- Option 2:  
Keep 4 subpixel buffers at normal resolution
  - ▣ Only update one of them each frame 😊

High-resolution buffer

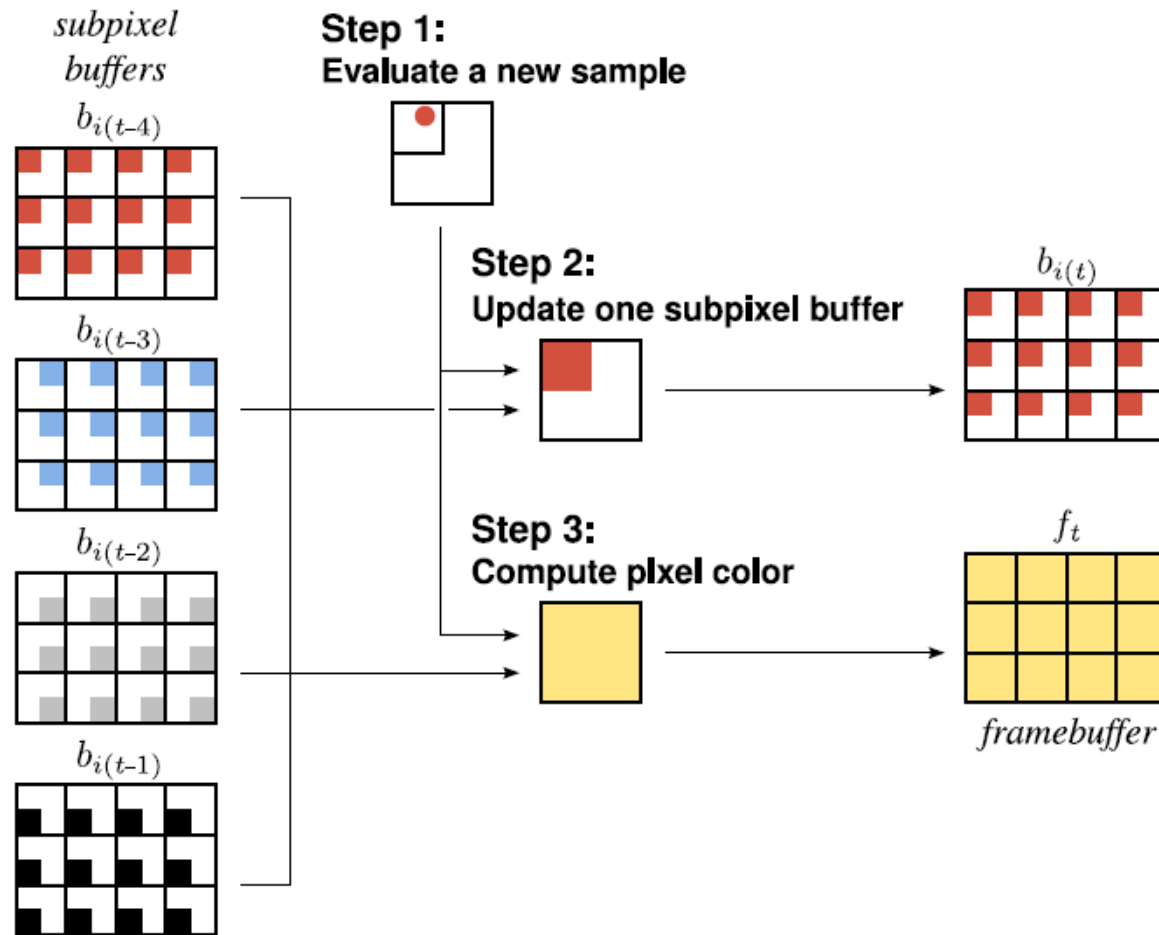


Subpixel buffers



# Subpixel buffers

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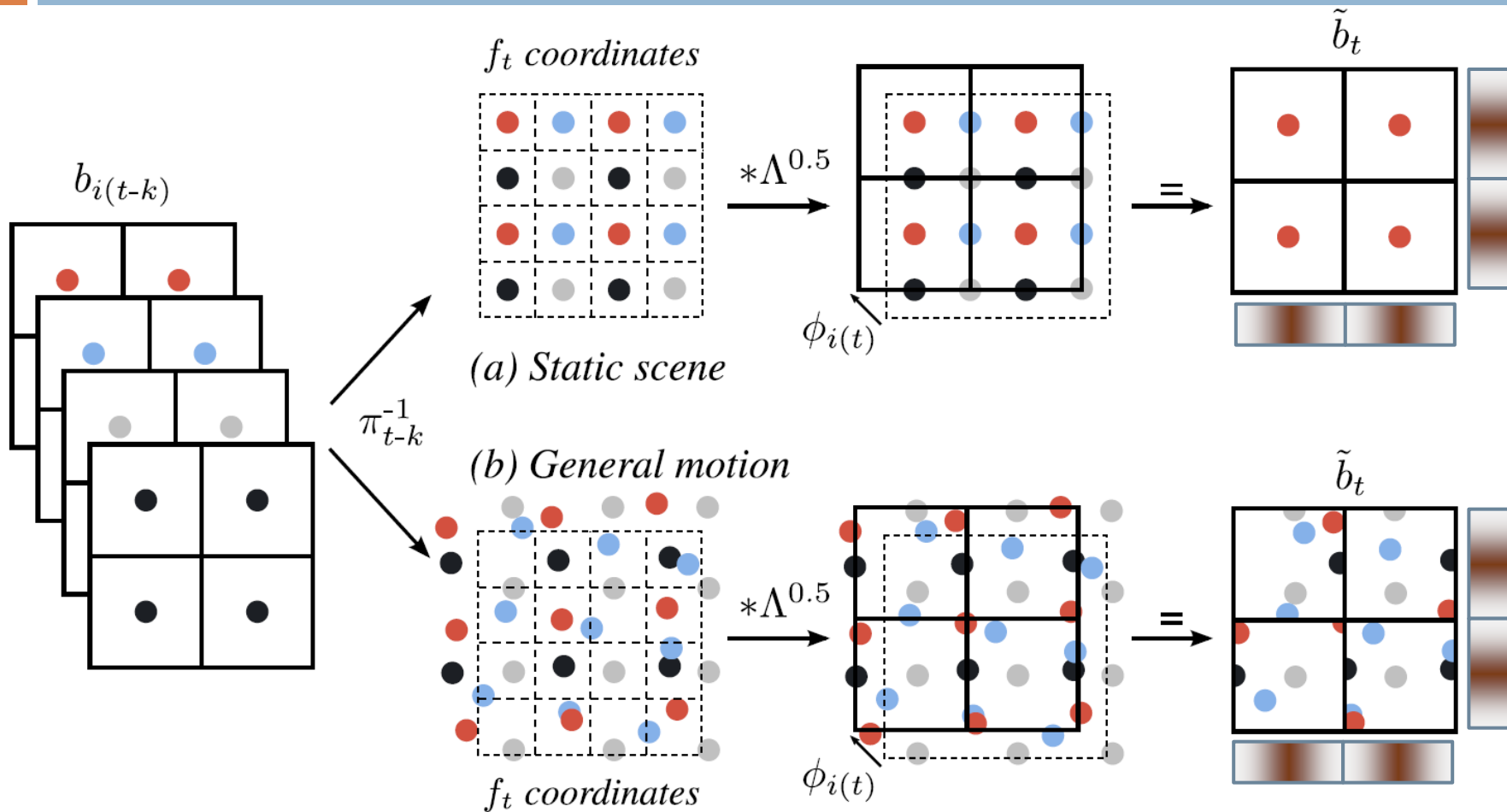
## (2) Avoid bilinear sampling

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- ▣ Reconstructing from subpixel buffers
  - ▣ Forward reproject the samples from 4 subpixel buffers to the current subpixel quadrant
  - ▣ Weight them using a tent function
  - ▣ GPU approximation/acceleration

# Reconstruction scheme

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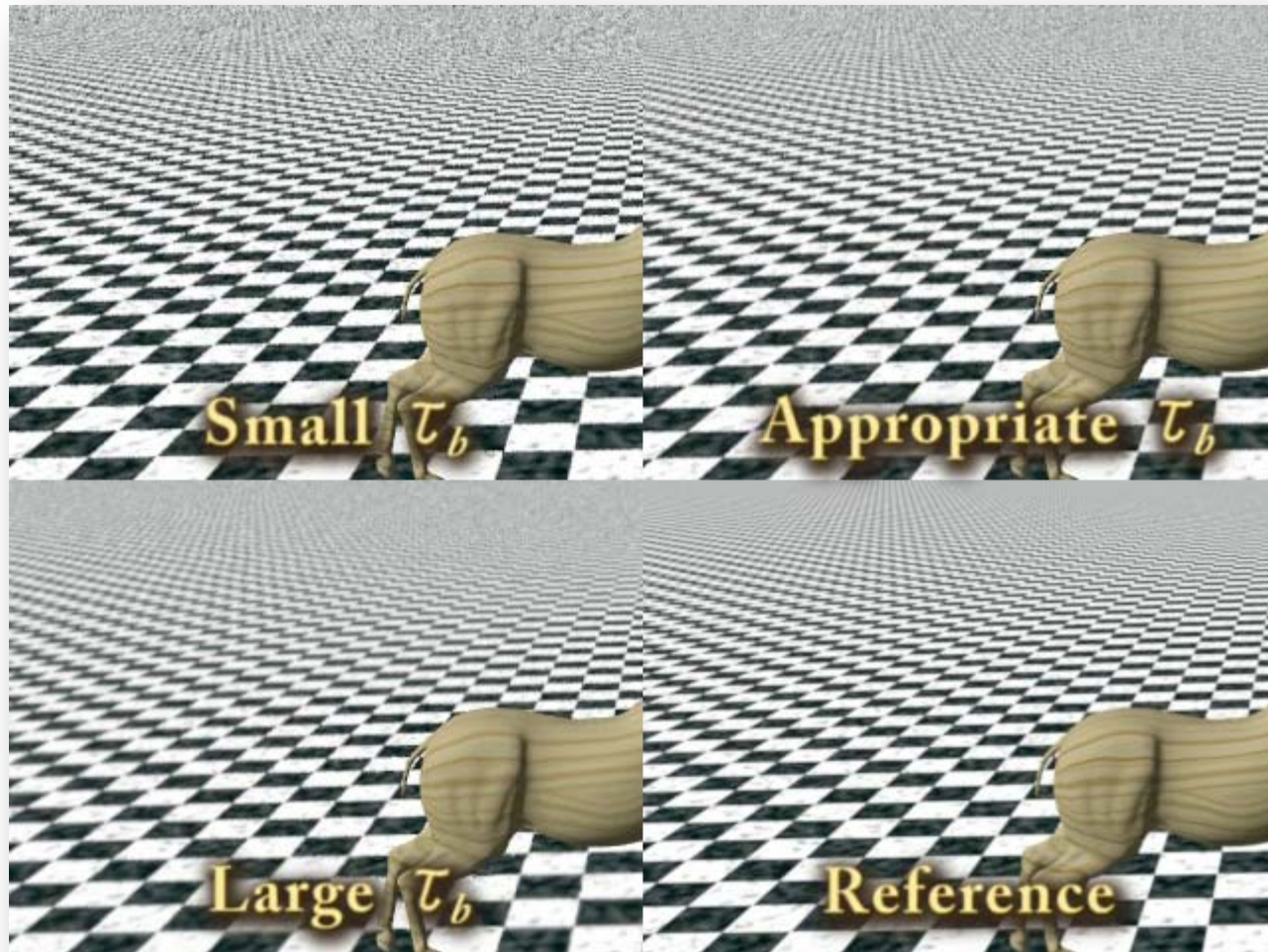
# (3) Limiting blur via bounding $\alpha$

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- Derive a relationship between
  - Blur variance  $\sigma^2$
  - Motion velocity  $v$  and  $\alpha$
- Analytic relationship is not attainable
  - Numerical simulation and tabulate
- Bound  $\alpha$  for limiting  $\sigma^2$  no larger than  $\tau_b$

# Tradeoff of blur and aliasing

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# Adaptive evaluation

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- Newly disoccluded pixels are prone to aliasing
- Additional shading for subpixels that fail in reconstruction



(a) Eval map



(b) One eval



(c) Adaptive eval



(d) Reference

# Accounting for signal changes

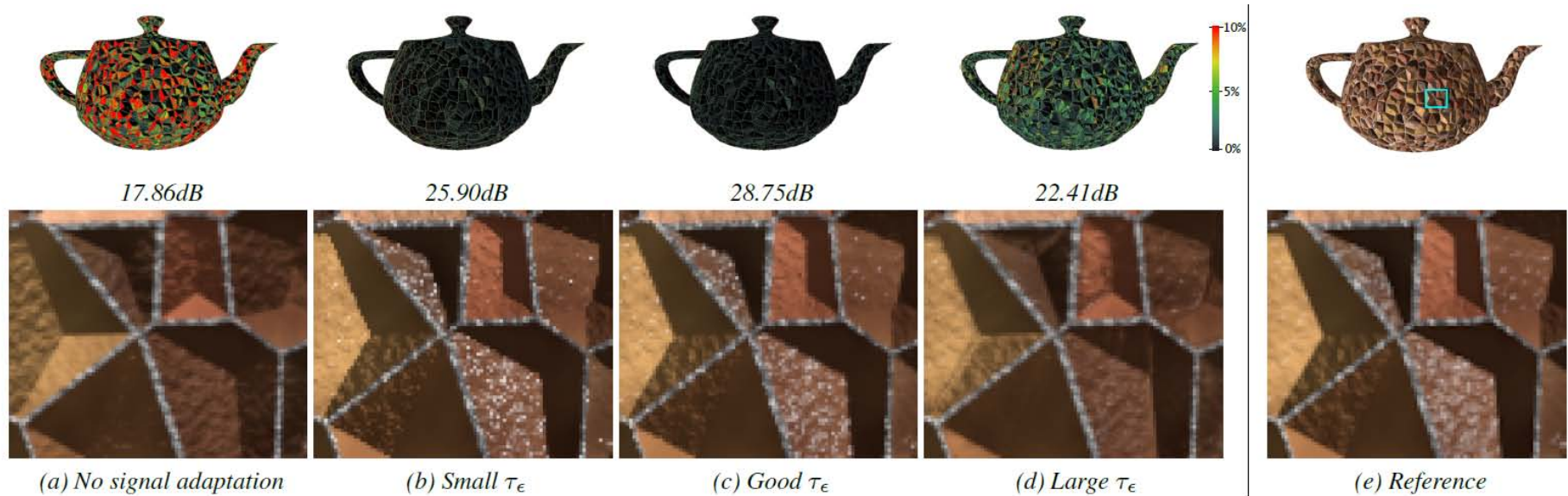
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- Detect fast signal change
  - React by more aggressive update
- Estimate residual  $\varepsilon$  between:
  - Current sample  $s_t$  (aliased/noisy)
  - History estimate  $f_t$
- Blur the residual estimate to remove aliasing/noise
- Bound  $\alpha$  for limiting  $\varepsilon$  no larger than  $\tau_\varepsilon$



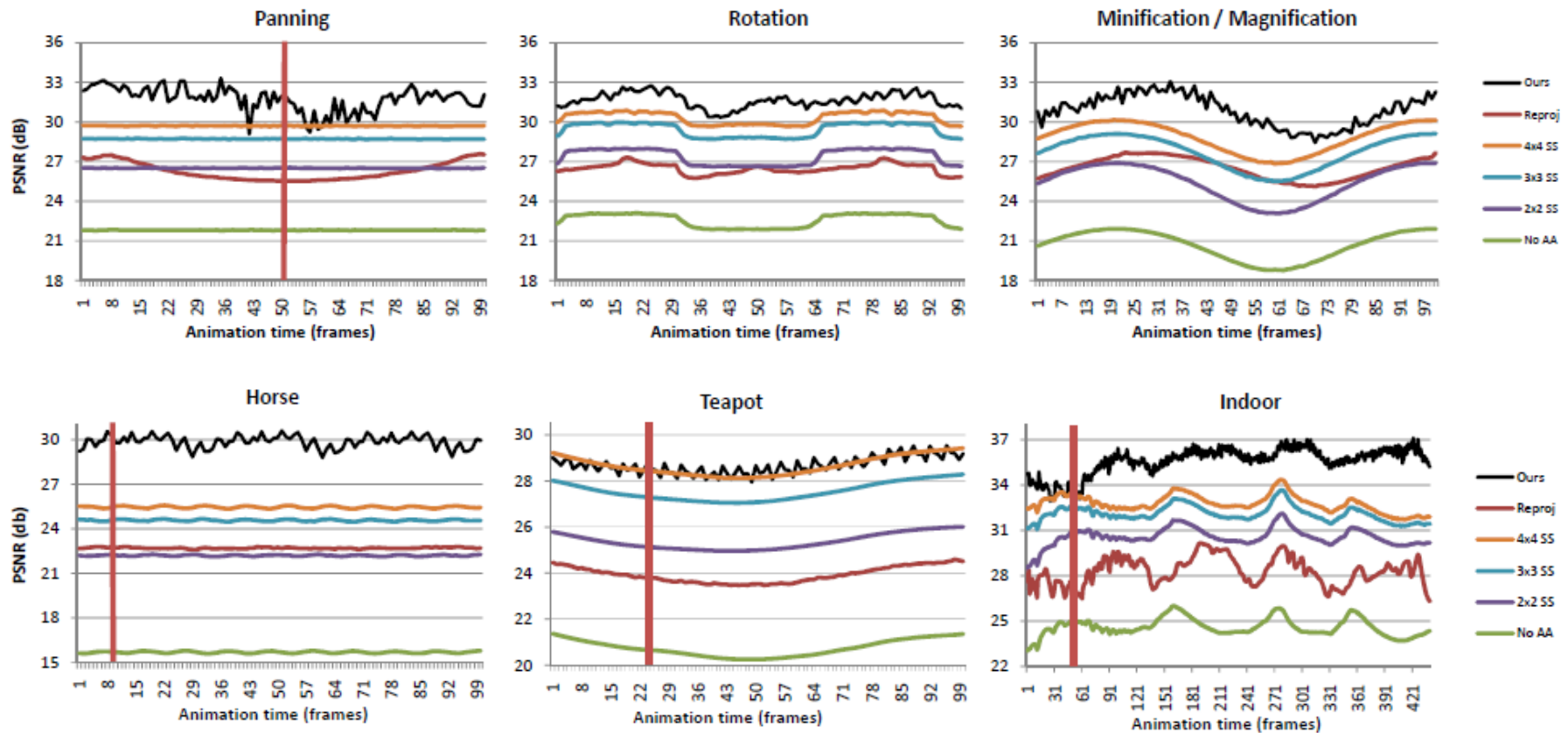
# Tradeoff of signal lag and aliasing

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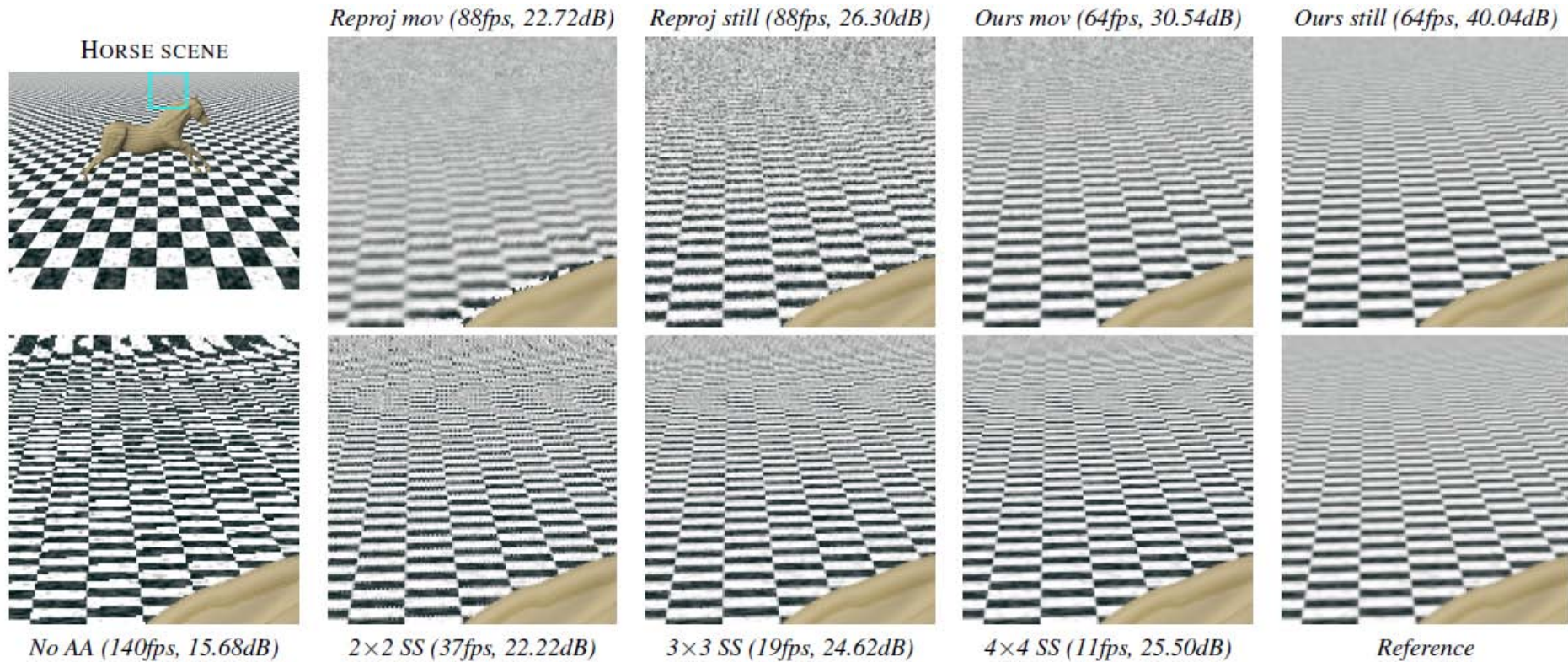
# Results

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# Results

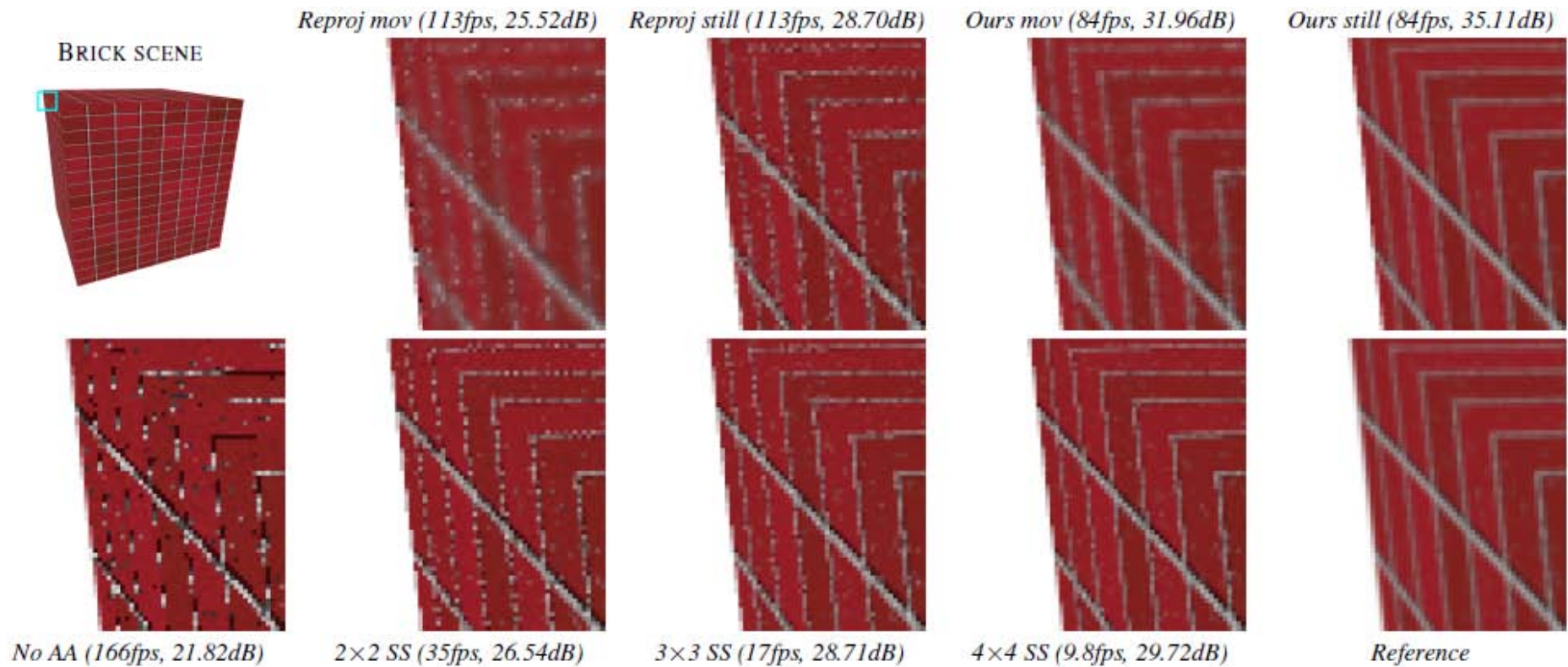
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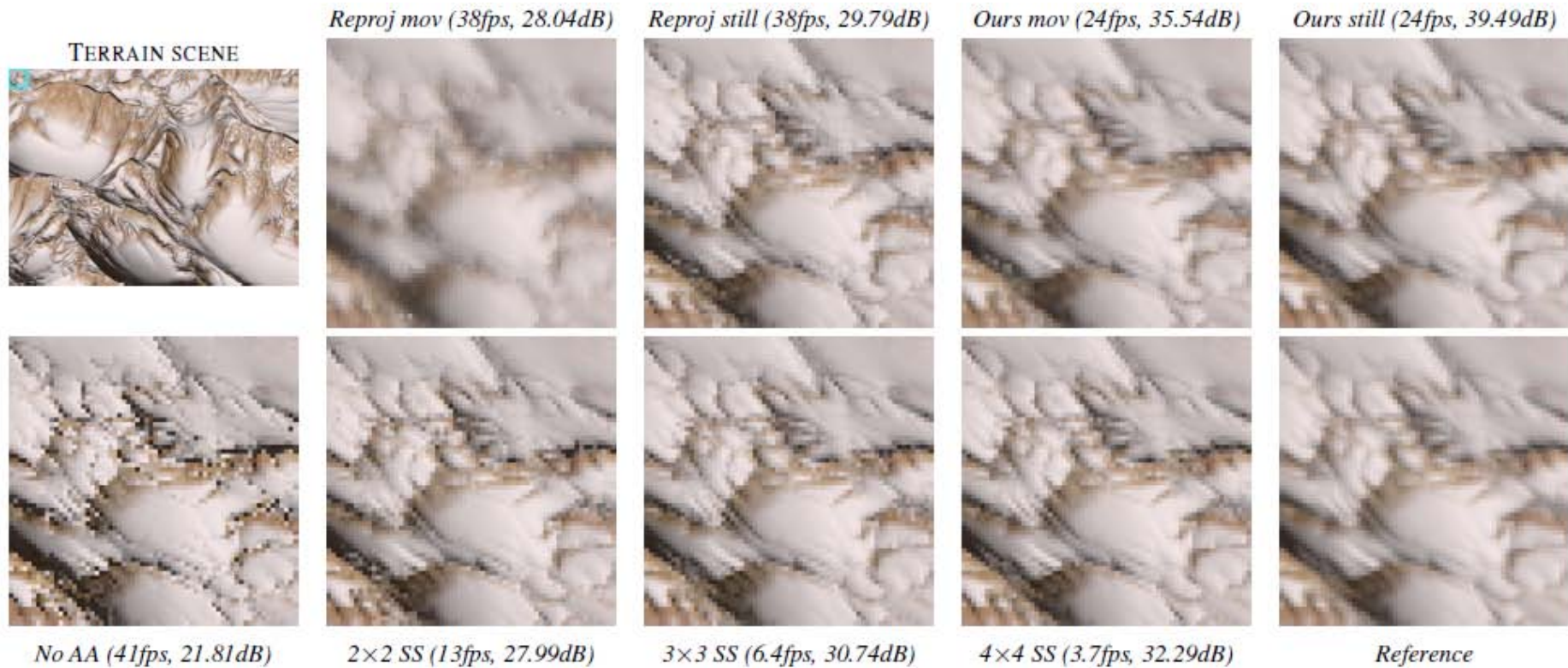
# Results

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# Results

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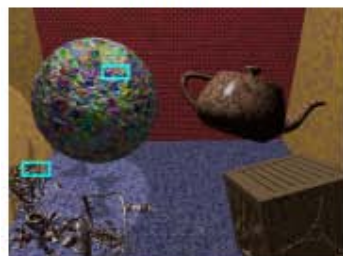




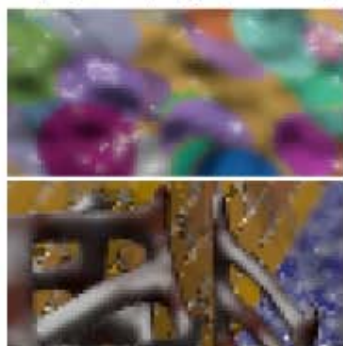
# Results

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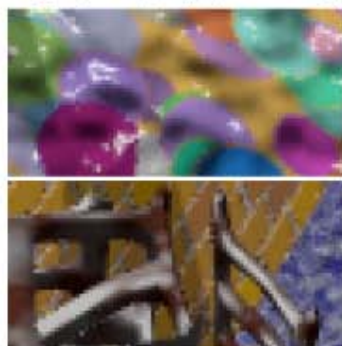
INDOOR SCENE



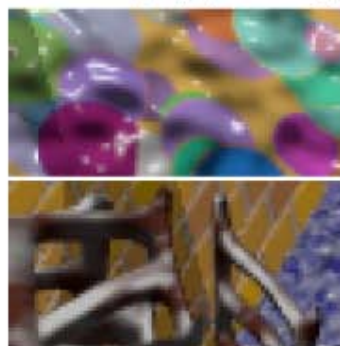
*Reproj mov (92fps, 27.27dB)*



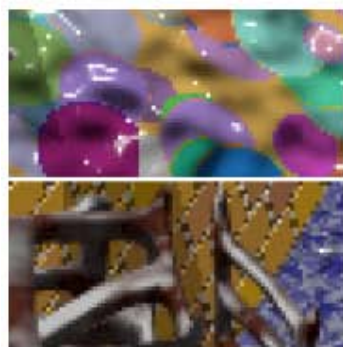
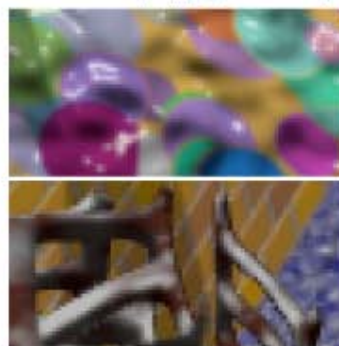
*Reproj still (92fps, 31.24dB)*



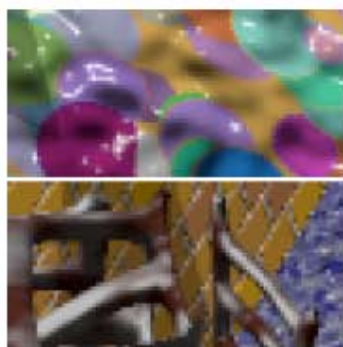
*Ours mov (52fps, 33.93dB)*



*Ours still (52fps, 38.37dB)*



*No AA (112fps, 24.79dB)*



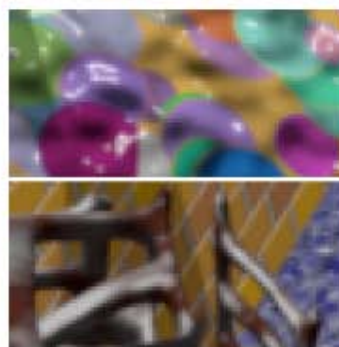
*2×2 SS (35fps, 30.33dB)*



*3×3 SS (17fps, 32.38dB)*



*4×4 SS (10fps, 33.26dB)*



*Reference*

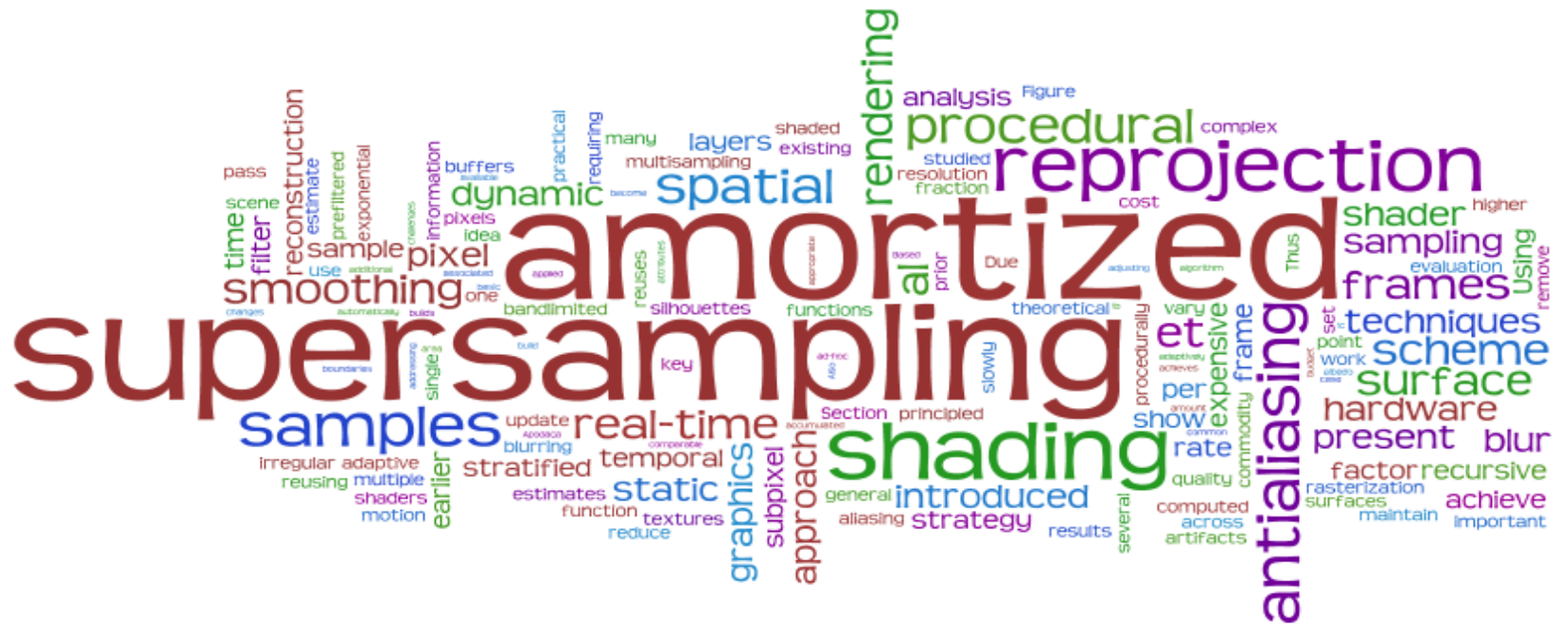


# Conclusion

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- A real-time scheme for amortizing supersampling costs
  - Quality comparable to 4x4 stratified supersampling
  - Speed is 5x-10x of 4x4 supersampling
  - A single rendering pass
- Future work
  - A broader range of temporal effects
  - Edge AA and motion blur

# Questions?



# GPU acceleration for reconstruction

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- Forward-reproject 16 samples to the tent  $\rightarrow$
- Reverse-reproject the tent to 4 subpixel buffers
  - A single bilinear fetch in each

